A Comparison of Image Denoising Methods using Wavelet, Contour let and Curve let Multi Resolution Transforms

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***Abstract*—**Image Processing is any form of signal processing for which the input is an image or video frame; the output of image processing is set of parameters related to the image. The goal of our research presents Denoising using various multi-resolution transforms (MRA) such as wavelets, Contourlets and Curvelets. Curvelet based image denoising method is compared with Wavelet denoising and contourlet denoises. The analysis shows that Curvelet performs better than wavelet and contourlet because the no. of co-efficient needed to represent a curve is lesser in Curvelet than Contour let and then Wavelet. Hence the computational complexity has also been reduced when using Curvelet transform.

***Keywords*—**Multi Resolution Analysis, Fourier Transform, Gaussian Scale Mixture, Wavelet Transform, Contourlet Transform, Curvelet Transform.

I. Introduction

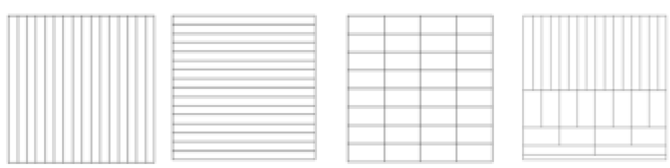
Wavelets are widely employed in signal and image processing for the past twenty years. A wavelet may be a mathematical relation helpful in digital signal processing and compression. The use of wavelets for these functions may be a recent development, though the speculation isn't new. [22]The principles are just like Fourieranalysis that was initially developed within the early part of the nineteenth century. In signal processing, wavelets create an attainable to recover weak signals from noise.This has proved particularly within the process of X-ray and magnetic-resonance pictures in medical applications.[25] Image processed during this approach are often "cleaned up" while not blurring or muddling details.Wavelet compression works by analysing a picture and changing it into a group of mathematical expressions that may be decoded by the receiver. A wavelet-compressed image file is usually given a reputation suffix of "WIF." Either your browser should support these files or it will need a plug-in program to browse the files. Most of the denoising methods work in the spatial domain whereas the MRA analysis works in both the time and frequency domain [1]. If wavelet transform is exploited [3] then the noise can be overcome even completely. Adaptive denoising methods also yield better results [6] and adopting spatial adaptively to a patch of pixels [10] providesimprovement. A Bayesian framework [11] along with a joint conditional model with the prior model as Anisotropic Markov random field demonstrates an improved denoising performance. Nonlinear filteing techniques [12] based on the theory ofrobust estimation yields deterministic and asymptotic properties in the presence of Gaussian and highly tailed noise. A nonlinear filter like Tri-state median filter also preserves most of the image details and suppresses the impulse noises [15].

II. Wavelet Transform and Multi-scale Analysis

Main theme of wavelet transforms:

- Frequency information is not available in time domain.
- Time information is not present in the Fourier transform model.

Seeking out an appropriate illustration of the information which will facilitate an analysis procedure is the basic issue in signal processing[19]. A method to realize this goal is to use transformation, or decomposition of the signal on a group of basic functions beforeprocessed within the transform domain.[26]Various transform models as shown in Fig. 1. Transform theory has a key role in image processing for variety of years, and it continues to be a subject of interest in theoretical additionally as applied to this field.



(a) (b) (c) (d)

Fig.1 Different transform model , (a) discrete sampling(no frequencylocalization) (b)Fourier Transform(no temporal localization) (c)Windowed fourier transform(constant Heisenberg boxes)(d)wavelet transform(variable Heisenberg boxes).

Image transforms used in several image processing fields, together with image restoration, encoding and description. If correlations between wavelet coefficients are studied carefully [4] then a better denoising technique can be produced. A parameterization of the denoise method [5] may also yield a lesser Mean Square Error (MSE). A variation of the wavelet coefficients is used in the shrinkage algorithm [13] and if scale and space consistency is also taken into consideration then there is improvement in the denoising performance [14].

A. Continuous Wavelet Transform

Continuous wavelet transform is a complexity mesh of the input data sequence with a bunch of function generated by a mother wavelet. The continuous wave rework could be a two-dimensional illustration.[28] This means the existence of redundancy which will be reduced[28] and even removed by sub-sampling the dimensions parameter and translation parameter.

B. Multi-scale Representations

Wavelet transforms [9][1][18]are a part of a general framework of multi-scale analysis.Variedmulti-scale representations are derived from the spatial-frequency framework, several of that introduced to produce additional flexibility for the spatial- frequency property or higher adaptation to universe applications. Unlike deuce wavelet transform,[27] moving wavelet transformation packet decompose the low frequency element, also because,the high frequency element in each sub-bands.

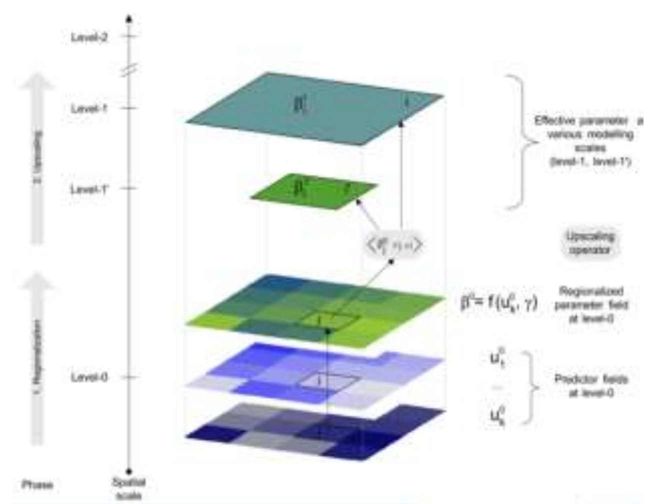


Fig. 2 Multi-scale analysis for spatial frame work

A sequence of agglomerative [19]case is mainly used to combine a missed data into a new cluster and it's continuously executer to recover the weak signal into a new one[27]. Fig. 3 shows spatial frame work to recover the neighbour data by the way of cluster formation.

III. RELATED WORK

The purpose of this methodology [7]is to summarize the usefulness of wavelets in various problems of medical imaging. WT is one of a best tool for us to determine where the low frequency area and high frequency area.After the compression techniques we neglect the weak signal at the same way of edge detection.

A. wavelet decomposition

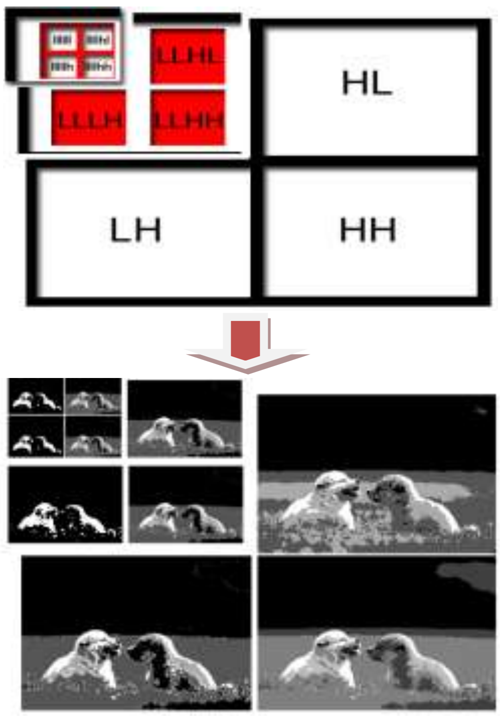


Fig. 3Wavelet decomposition process for four level of technique (1) low-high (2) high-low (3) high-high.

Originally known as most advantageous Sub band tree structuring (SB-TS) [2] also called wavelet packet decomposition[25] (WPD) (sometimes known as just Wavelet Packets or Sub-band Tree) is a wavelet transform where the discrete-time (sampled) signal is approved through more filters than the discrete wavelet transform (DWT) [22][25].

For n levels of decomposition the WPD produces 2n different sets of coefficients (or nodes) as opposed to (3n +1) sets for the DWT.[22] However,dueto the downsampling process the overall number of coefficients is still the same and there is no redundancy.Discrete Wavelet Transform theory[22] (continuous within the variable(s)) associate approximation to remodel sampled signals. In addition, the separate sub band transform theory provides an ideal illustration of separate signals.

B. wavelet transform

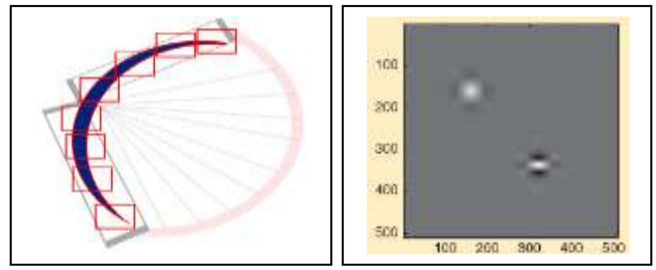


Fig. 4Wavelet transform edge detection method and Wavelet translation in spatial domain

A filter bank structure which will deal effectively with piecewise pictures [18]with contours. The resulting image enlargement may be a directional multi resolution analysis[24] framework composed by contour segments, and therefore is called Contourlet. In this wavelet transform[26]easily identifying some time and frequency domain and noisy signal.

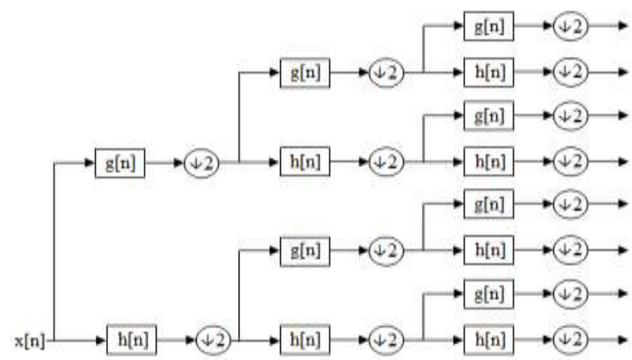


Fig.5Down sampling and Up sampling of the Wavelet Co-efficients

Wavelets generalize the Fourier transform by using a basis that represents both location and spatial frequency. For 2D or 3D signals, directional wavelet transforms go further, by using basis functions that are also localized in orientation.

C. Selection of Threshold Value

Given the fundamental framework [7]of de-noising persecution, wave thresholding as mentioned within the previous sections,[29][30]it clear that the edge level parameter T plays a vital role. Values too small cannot effectively get obviate noise part,[29]whereas values overlarge can eliminate helpful signal elements.

D. Contourlet Transformation

Contourlet transformation [20][21]captures smooth contours and edges at any orientation,filters the noise and reduce unwanted signal, derived directly from discrete domain instead of extending from continuous domain. It can be implemented using filter banks.

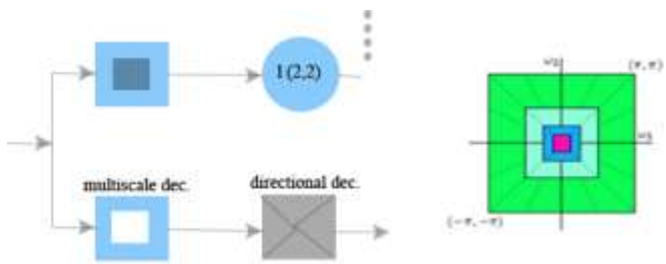


Fig. 6Contourlet filter bank, (a) Frequency partitioning, (b) The multichannel view of an l-level tree-structured directional filter bank

The transform decouples [20]the multi-scale and the directional decompositions process as shows on Fig.6.

The multi-scale decomposition is handled by a Laplacian pyramid and the directional decomposition is handled by a directional filter bank as shown in fig.6. This contourlet transform's main theme is best way of identifying edge-detection of required image.Directional filter bank and multi-scale decomposition both of this area are important place in contourlet filter bank. Directional filter bank woks to absorb the high frequency of a given input image shown in fig. 3, and low frequency could not absorb properly by this (DFB)Directional filter bank.

The Collection of low frequency [8]would 'leek' and allow into some directional sub-band. So for this condition directional filter bank does not do the parse representation on an appropriate image. Thus the low frequency value of the input images is neglected before applying directional filter bank. This is the reason for combining DFB with multi-scale decomposition. Fig. 5(a) shows a multi-scale decomposition and directional decomposition Process using a combination of a Laplacian pyramid (LP) and adirectional filter bank (DFB).

Thus the combined result is a double iterated filter bank structure, called as contourlet filter bank,which decomposes images into directional sub-bands at multiple scales.

Contourlet transform can easily identifying edge of that particular image, so retrieve the low signal can easily identified using contourlet transformation.

E. Curvelet Transformation(ProposedSystem)

Being the extension [16][17][18]of wave, curvelet transformation did form a spectacular performance in image denoising and also the result shows that it performs a better in image denoising. The traditional strategies for image denoising are "frequency filtering" and "frequency smoothing".[24] Those two strategies have a similar disadvantage that the process can lose uncountable image information. Once applying the second wave transform to an image,several constant was required the edges.[24] If we tend to reconstruct the sting of image, it will take uncountable memory. However the curvelet transform overcome this disadvantage that it takes few nonzero coefficients to explain the sting,

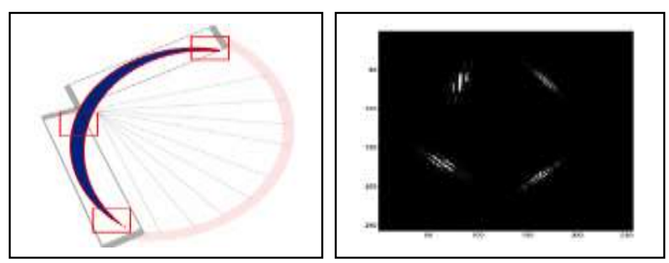


Fig.7Curvelet transform for edge detection

This shows why it is better than wavelet as image denoising[18]. We can find that the performance of the curvelet transform reach is very good. With the help of image denoising, it is able to identify detail information of the SAR image. This technology is powerful and useful. So using this method it is possible for maintaining image quality of denoising method using the Multi Resolution [24] Analysis Transforms.

IV. EXPERIMENTAL RESULT

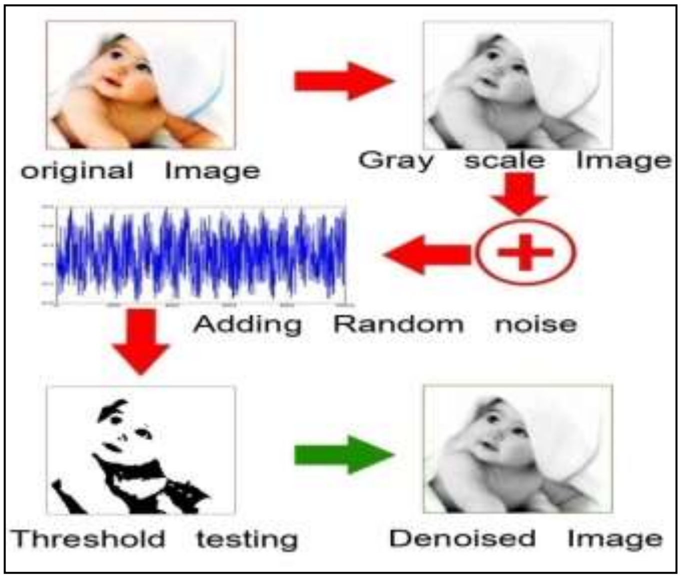


Fig .8 Flow diagram for curveletdenoising method and various stages of performance

The original image is regenerate to the gray scale so random noise is applied as shown in Fig. 8.Finally, SNR price is calculated using totally different threshold values for the wavelet transform. This approach is mostly easy and effective.The process for the duration of these algorithms iscarried within the transformation domain. During this approach, the distinct wavelet transform (DWT) of an indication is calculated.

During this case,the coefficients that are smaller than a definite value are removed [5]. Then, the resultantcoefficients will reconstruct the signal.

Fig. 9 Image of experimental result of Signal to noise ratio (9.55db,10.36db,14.19db,18.72db,19.10db,18.38db) for different threshold level(1,2,3,4,5) in wavelet Denoising.

With this technique, it's doable to obtain noise with very little loss of details. If an indication has its energy targeted in a very tiny range of wavelet coefficients, its constant values are comparatively enormous compared to the noise that has its energy adjoin an outsized range of coefficients. The subsequent figures show the result of the wavelet transformation [24] with Thresholds 1-5.

A. Threshold For wavelet noise removal

A graph showing the Average threshold Vs Signal to Noise Ratio (SNR) was drawn and found that a threshold values threshold = 3 is optimum. The table used for the plot is also listed here.

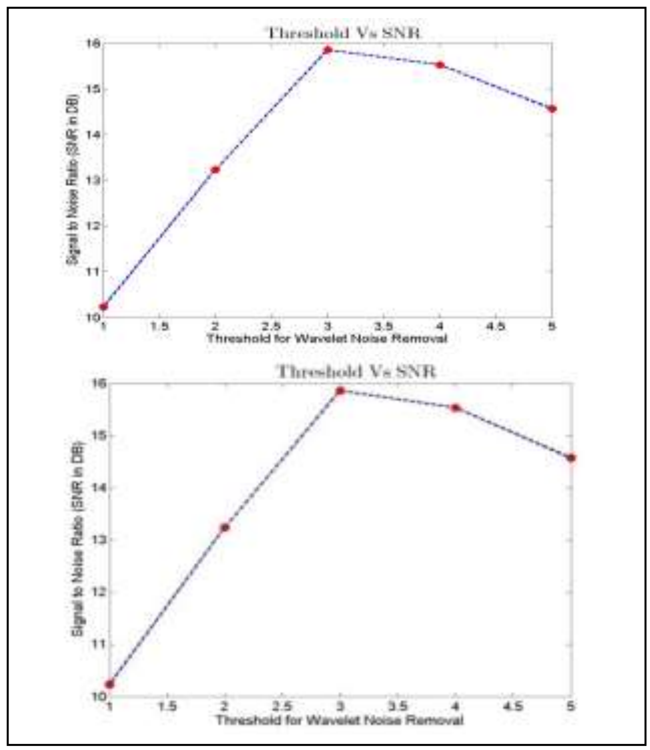


Fig. 10Graph for signal to noise ratio in y axis and wavelet threshold for x axis

Above fig . 10 shows the values is the combination of signal to noise in y-axis , and threshold in x axis. Different threshold values are placed in the side of the graph with different threshold [29][30] and signal to noise ratio.Plot the different threshold values (1, 2,3,4,5) inside the table, and this combination is mainly used to compare the threshold value one to another because of getting absolute output.

Image No	Noise DB	SNR for Threshold =				
		1	2	3	4	5
1	9.53	10.09	12.22	13.31	12.73	11.96
2	9.55	10.23	13.08	15.25	14.93	14.17
3	9.55	10.10	12.24	13.43	12.89	12.15
4	9.53	10.18	12.89	14.84	14.42	13.65
5	9.57	10.13	12.28	13.38	12.75	11.98
6	9.56	10.25	13.12	15.09	14.43	13.56
7	9.55	10.29	13.71	17.20	17.33	16.60
8	9.54	10.27	13.64	16.71	16.40	15.45

Table.1Mean values for different threshold level

V. CONCLUSIONS

In this project, several issues were addressed to improve image denoising and the comparison graph is plotted as shown in fig. 11, from this graph the SNR value for multiresolution analysis technique is calculated. Signal to noise ratio values for various transforms are determined, they are, wavelet transformation SNR value is 10.23, SNR value of Contourlet transformation is 10.99,SNR value of Curvelet transformation is 17.66. By this analysis it can be concluded that Curvelet transform is the best one to reducing noise level from a noisy image.

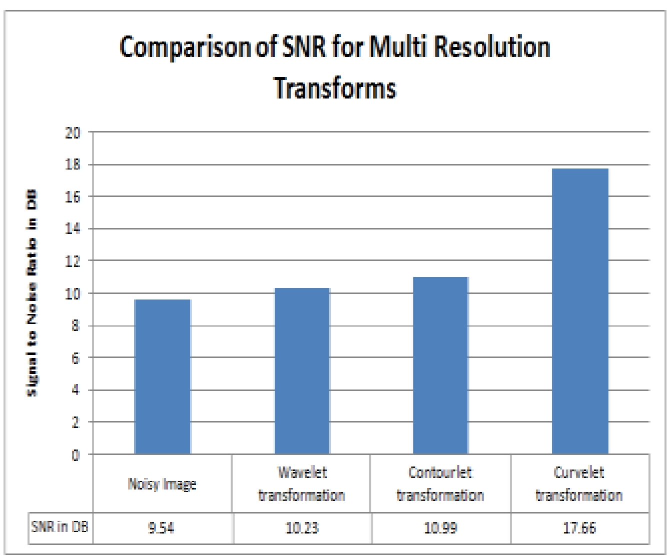


Fig . 11 Comparison of SNR for multi resolution analysis transforms.

Curvelet transforms signal level is too high so it can easily reduce the noise level than another transformation. Multiresolution [24] noise ratio is calculated as shown in fig. 11. By this analysis, it is clear thatcurvelet transform is the best one to reduce the noise level and noise ratio is calculated by using 200 images with different threshold [30] , size, noise level values.

In this multiresolution analysis system compared with three transformation, they are curvelet, contourlet and wavelet transform. Among these process curvelet transformation is best one for denoising process as shown in fig. 11.

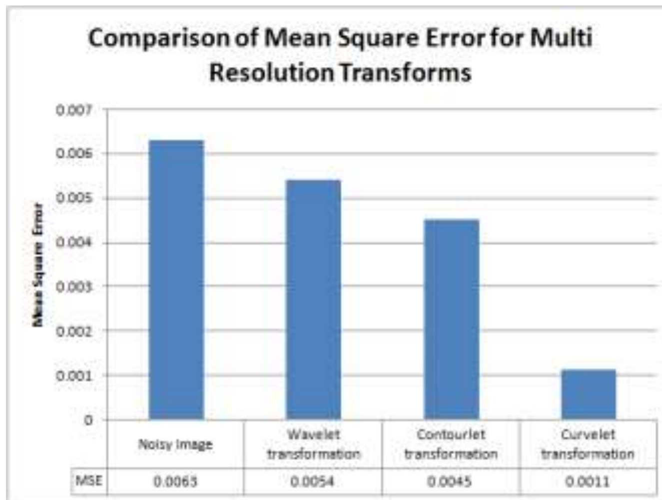


Fig . 12 comparison of Mean square error for multi resolution analysis transforms.

Mean square error is calculated by the comparison of wavelet, Curvelet and contourlet transformation as shown in fig. 12. Curvelet transform is the best than wavelet and contourlet transform to suppress the noise.

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